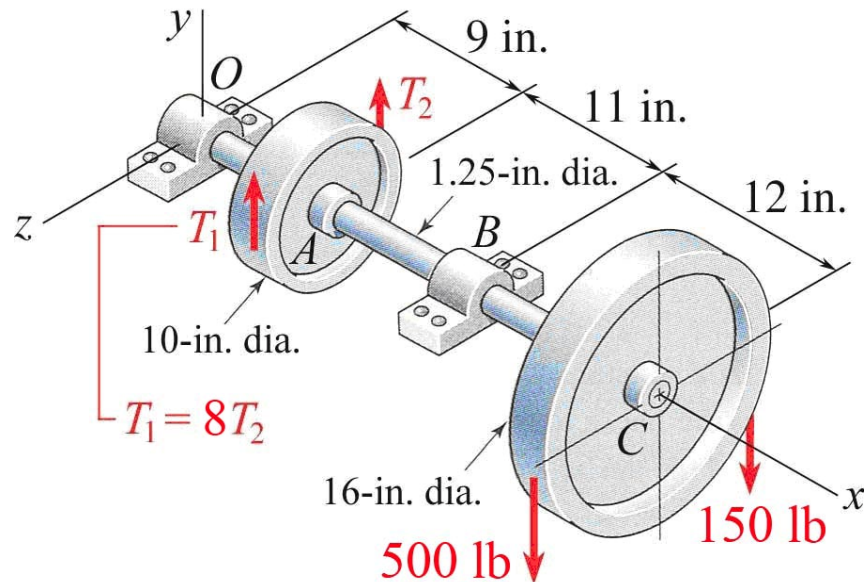


**MEEG 4103 Quiz 4.1c.081** A steel countershaft with roller bearings at  $O$  and  $B$  is in equilibrium as shown, where  $T_1 = 8T_2$ . Taking the bearings as simple supports, determine (a) the deflection  $y_C$  at  $C$ , (b) the minimum shaft diameter  $d_{\min}$  needed, using  $\frac{1}{8}$ -in. increments, if the slope at either bearing should not exceed  $0.07^\circ$ , (c) the value of  $y_C$  when the shaft diameter is  $d_{\min}$ .



$$E = 30 \times 10^6 \text{ psi} \quad I = \frac{\pi}{4} r^4 \quad T_1 = 640 \text{ lb} \quad T_2 = 80 \text{ lb} \quad \textcircled{1}$$

$$\text{In FBD } \textcircled{1} \text{ for shaft: } \mathbf{O}_y = 786 \text{ lb} \downarrow \textcircled{1} \quad \mathbf{B}_y = 716 \text{ lb} \uparrow \textcircled{1}$$

$$\text{In FBD for CB: } \textcircled{1} \quad O_y^c = \frac{44\,414}{EI} \quad M_C^c = -\frac{1\,205\,112}{EI}$$

$$(a) \quad 2r = d = 1.25 \text{ in.} \quad y_C = M_C^c \quad y_C = -0.335 \text{ in.} \quad \textcircled{1}$$

$$(b) \quad \text{At } O: \theta_O = V_O^c = O_y^c \leq 0.07\pi/180: \quad d \geq 2.229 \text{ in.} \quad \textcircled{1}$$

$$\text{At } B: \theta_B = V_B^c, \quad |V_B^c| \leq 0.07\pi/180: \quad d \geq 2.491 \text{ in.} \quad \textcircled{1}$$

$$\text{Use } d_{\min} = 2\frac{1}{2} \text{ in.} \quad \textcircled{1} \quad (c) \quad y_C = -0.0209 \text{ in.} \quad \textcircled{1}$$