## MEEG 4103 Quiz 6.3.081

## (Closed book, closed notes)

- In the σ<sub>a</sub>' versus σ<sub>m</sub>' plane, carefully draw the lines and write the equations for the following fatigue failure criteria:
  (a) Soderberg line, (b) modified Goodman line, (c) ASME-elliptic line, (d) Gerber line, and (e) Langer yield line.
- 2. ② A shaft has the properties  $S_e = 300$  MPa,  $S_y = 480$  MPa, and  $S_{ut} = 620$  MPa. The shaft is subjected to an alternating bending stress of 120 MPa, an alternating torsional stress of 90 MPa, and a steady torsional stress of 80 MPa. Find the factor of safety  $n_y$  guarding against a static failure.
- **3**. ③ For the shaft in Problem 2, find the factor of safety  $n_f$  guarding against a fatigue failure using (*a*) modified Goodman line, (*b*) ASME-elliptic line, (*c*) Gerber line.
- **1.** (SMAG Lines from GA to MS and equations)  $1 \times 5 = 5$
- 2.  $\sigma'_{\text{max}} = 317.96 \text{ MPa}$   $n_y = S_y / \sigma'_{\text{max}} = 1.5096$   $n_y = 1.51$

3. 
$$\sigma_a' = \frac{1}{\sqrt{2}} \left[ 2 \sigma_a^2 + 6 \tau_a^2 \right]^{1/2} = 196.723 \text{ MPa}$$

$$\sigma'_{m} = \frac{1}{\sqrt{2}} \left[ 6\tau_{s}^{2} \right]^{1/2} = 138.564 \text{ MPa}$$

- (a) Modified Goodman line:  $n_f = 1.14$  ①
- (b) ASME-elliptic line:  $n_f = 1.40$  ①
- (c) Gerber line:  $n_f = 1.38$  ①