

MEEG 4703 [Quiz M3.073](#)

1. (10 points) Find the eigenvalues and eigenvectors of the matrix \mathbf{A} shown.

$$\mathbf{A} = \begin{bmatrix} 5 & 1 & 0 \\ 0 & 5 & -9 \\ -5 & -1 & 0 \end{bmatrix} \quad \mathbf{B} = \begin{bmatrix} -2 & 2 \\ -2 & 3 \end{bmatrix}$$

2. (10 points) Using Cayley-Hamilton theorem, compute \mathbf{B}^{11} for the matrix \mathbf{B} shown.
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1. $\lambda_1 = 0, \lambda_2 = 2, \lambda_3 = 8$

$$\mathbf{K}_1 = \begin{bmatrix} -9 \\ 45 \\ 25 \end{bmatrix}, \quad \mathbf{K}_2 = \begin{bmatrix} -1 \\ 3 \\ 1 \end{bmatrix}, \quad \mathbf{K}_3 = \begin{bmatrix} 1 \\ 3 \\ -1 \end{bmatrix}$$

2. $\lambda_1 = -1, \lambda_2 = 2; c_0 = 682, c_1 = 683$

$$\mathbf{B}^{11} = \begin{bmatrix} -684 & 1366 \\ -1366 & 2731 \end{bmatrix}$$