

Ph.D. Qualifying Exam – Statics, Dynamics, & Vibrations (Fall 2010)

Closed books & closed notes

Name: \_\_\_\_\_

(Time: 2 hours)

ID #: \_\_\_\_\_

- Determine the axial forces  $F_{AB}$ ,  $F_{BC}$ , and  $F_{FG}$  in members  $AB$ ,  $BC$ , and  $FG$  of the compound truss as shown in Fig. 1. Use  $T$  or  $C$  to indicate whether each of these forces is a *tensile* force or *compressive* force.

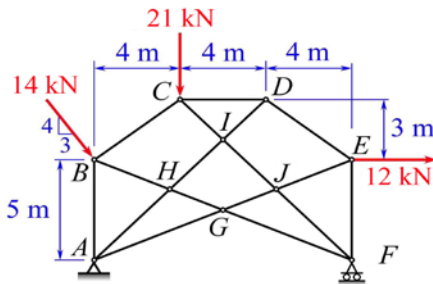


Fig. 1

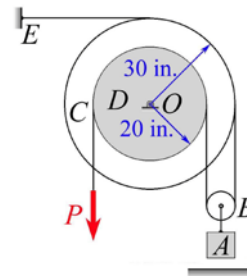


Fig. 2

- Two drums  $C$  and  $D$  are rigidly fastened together and are free to rotate about the bearing at  $O$  as shown in Fig. 2. The coefficient of static friction  $\mu_s$  is 0.12 between the belt and all surfaces of the drums. Determine the minimum magnitude  $P_{\min}$  of the applied force  $\mathbf{P}$  required to prevent the 80-lb block  $A$  from falling down to the ground.
- A section of pipe weighing 48.3 lb rolls without slipping with angular velocity  $\omega_1$  before falling into a 14-in. gap (a pot hole) as shown in Fig. 3. If impact at the gap is perfectly plastic and the pipe rolls with  $\omega_2 = 4 \text{ rad/s}$  after having climbed up the gap to the other side, determine its angular velocities (a)  $\omega''$  just after impact, (b)  $\omega'$  just before impact, (c)  $\omega_1$ .

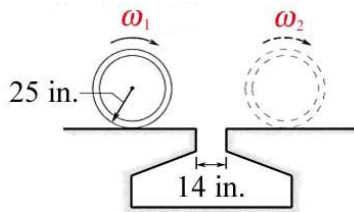


Fig. 3

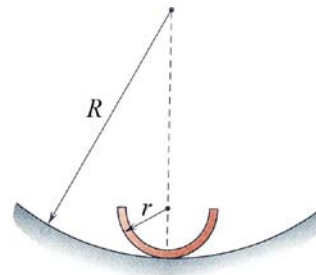


Fig. 4

- A section of thin semicircular shell of mass  $m$  and mean radius  $r$  rests at the bottom of a cylindrical surface of radius  $R$  as shown in Fig. 4. If the shell rocks without slipping on the surface, determine its frequency of small-amplitude vibration.