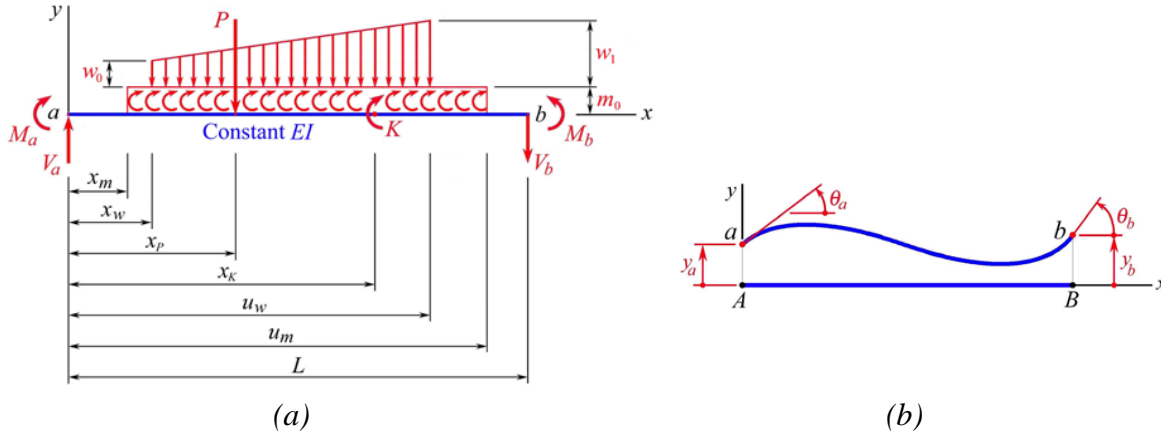


Excerpt from the Method of Model Formulas

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icjong@uark.edu



Positive directions of forces, moments, slopes, and deflections

$$\begin{aligned}
 y' = & \theta_a + \frac{V_a}{2EI}x^2 + \frac{M_a}{EI}x - \frac{P}{2EI}\langle x-x_p \rangle^2 + \frac{K}{EI}\langle x-x_k \rangle^1 - \frac{w_0}{6EI}\langle x-x_w \rangle^3 \\
 & - \frac{w_1-w_0}{24EI}(u_w-x_w)\langle x-x_w \rangle^4 + \frac{w_1}{6EI}\langle x-u_w \rangle^3 + \frac{w_1-w_0}{24EI}(u_w-x_w)\langle x-u_w \rangle^4 \\
 & + \frac{m_0}{2EI}\langle x-x_m \rangle^2 - \frac{m_0}{2EI}\langle x-u_m \rangle^2
 \end{aligned} \tag{1}$$

$$\begin{aligned}
 y = & y_a + \theta_a x + \frac{V_a}{6EI}x^3 + \frac{M_a}{2EI}x^2 - \frac{P}{6EI}\langle x-x_p \rangle^3 + \frac{K}{2EI}\langle x-x_k \rangle^2 - \frac{w_0}{24EI}\langle x-x_w \rangle^4 \\
 & - \frac{w_1-w_0}{120EI}(u_w-x_w)\langle x-x_w \rangle^5 + \frac{w_1}{24EI}\langle x-u_w \rangle^4 + \frac{w_1-w_0}{120EI}(u_w-x_w)\langle x-u_w \rangle^5 \\
 & + \frac{m_0}{6EI}\langle x-x_m \rangle^3 - \frac{m_0}{6EI}\langle x-u_m \rangle^3
 \end{aligned} \tag{2}$$

$$\begin{aligned}
 \theta_b = & \theta_a + \frac{V_a L^2}{2EI} + \frac{M_a L}{EI} - \frac{P}{2EI}(L-x_p)^2 + \frac{K}{EI}(L-x_k) - \frac{w_0}{6EI}(L-x_w)^3 \\
 & - \frac{w_1-w_0}{24EI}(u_w-x_w)(L-x_w)^4 + \frac{w_1}{6EI}(L-u_w)^3 + \frac{w_1-w_0}{24EI}(u_w-x_w)(L-u_w)^4 \\
 & + \frac{m_0}{2EI}(L-x_m)^2 - \frac{m_0}{2EI}(L-u_m)^2
 \end{aligned} \tag{3}$$

$$\begin{aligned}
 y_b = & y_a + \theta_a L + \frac{V_a L^3}{6EI} + \frac{M_a L^2}{2EI} - \frac{P}{6EI}(L-x_p)^3 + \frac{K}{2EI}(L-x_k)^2 - \frac{w_0}{24EI}(L-x_w)^4 \\
 & - \frac{w_1-w_0}{120EI}(u_w-x_w)(L-x_w)^5 + \frac{w_1}{24EI}(L-u_w)^4 + \frac{w_1-w_0}{120EI}(u_w-x_w)(L-u_w)^5 \\
 & + \frac{m_0}{6EI}(L-x_m)^3 - \frac{m_0}{6EI}(L-u_m)^3
 \end{aligned} \tag{4}$$